

The emergence of altruism as a social norm

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June 20, 2017

1 **Abstract**

2 Expectations, exerting influence through social norms, are a very strong candidate to explain
3 how complex societies function. In the Dictator game (DG), people expect generous behavior
4 from others even when they cannot enforce any sharing of the pie. Here we assume that people
5 donate following their expectations, and that they update their expectation after playing a DG
6 by reinforcement learning to construct a model that explains the main experimental results in
7 the DG. Full agreement with the experimental results is reached when some degree of mismatch
8 between expectations and donations is added into the model. These results are robust against
9 the presence of envious agents, but affected if we introduce selfish agents that do not update
10 their expectations. Our results point to social norms being on the basis of the generous behavior
11 observed in the DG and also to the wide applicability of reinforcement learning to explain many
12 strategic interactions.

13 In spite of the many fundamental issues that humanity still faces both at local and global
14 scales, human society has proven capable of taking our species to levels of adaptation and success
15 unrivaled in the animal world [1]. Research in evolutionary psychology and anthropology suggests
16 that human beings are especially social mostly because they are especially cooperative [2, 3]. One
17 of the main mechanisms behind such an ultra-cooperative behavior is expectations, that promote
18 prosocial behavior through the willingness to fit in the group (to conform to the expectations the
19 group has about oneself [4]) and/or to avoid punishment (for not following their expectations [5]).
20 According to Bicchieri [6], social norms are indeed governed by both empirical expectations (what
21 we believe others will do) and normative expectations (what we believe others believe we will do).
22 Thus, expectations which drive behavior become social norms [6] to which most people conform,
23 leading to an overall cooperative performance of the society [7, 8]. Social norms can serve to
24 choose among different Nash equilibria in social complex environments –games– where individuals
25 face strategic interactions [9, 10] and drive behavior in non-strategic settings where individuals can
26 choose actions depending on their expectations of others and the degree to which these actions are
27 seen appropriate [11].

28 A particularly well-suited framework to study expectations is the dictator game (DG for short),
29 which has provided a large body of experimental evidence on altruistic behaviour in the lab during
30 the last thirty years [12, 13]. The DG is a simple one-shot game with two players: the first one
31 (the dictator) is invited to divide a specified amount between herself and the second player (the
32 recipient). The dictator may divide the pie in the manner she sees fit, while the recipient is not
33 permitted to make any claim to the money. Theoretically, self-centered preferences predict that
34 the dictator keeps all the pie and the recipient receives nothing; hence, any positive donation
35 can be interpreted as proof of generosity. Contrary to the self-centered prediction, Engel’s meta-
36 analysis [12] shows that a huge number of individuals do offer nonzero, often sizeable portions of the
37 pie to the recipient. On average, subjects donate between 20-30% of the total pie with a non-trivial

38 fraction of subjects choosing an equal split. Interestingly, some authors argue that this is indeed a
39 lower bound for generosity given the absence of social context within a lab experiment [13–18].

40 Expectations in the DG have been recently studied in a series of experiments that allowed to
41 probe the influence of different social factors on the observations [19]. Specifically, we have found
42 that even if we elicit expectations from people in different roles, or from external observers of the
43 social interaction, or from subjects socially distant because they refer to a previous experimental
44 session, or when the money at stake is large, we always find that people expect generous behavior.
45 In fact, a majority of people expects a fair split and only about 10% of the subjects predict they
46 will receive nothing. On the other hand, people have a behavior that is very correlated with their
47 expectations, which supports the role of expectations in the formation of social norms (see also
48 Refs. 11, 20, 21).

49 In this paper, we model the formation of people’s expectations in terms of learning from own
50 experience, and in particular we focus on expectations in the DG in order to validate our model by
51 comparing to the large amount of available experimental evidence. We model behavior by assuming
52 that people’s decisions are based on what they expect and on what they observe. Subjects are thus
53 endowed with *aspirations* that reflect what they expect to gain from any interaction. In our setting,
54 aspirations of subjects coincide in value with expectations about the donations they will receive
55 as recipients; while when acting as dictators, we will posit that their donations are such that they
56 keep the money that corresponds to their expectations [see Eq. (4 below)]. The fraction of the pie
57 that recipients receive from dictators is compared with their aspiration level; when the donation is
58 larger (than expected) then the stimulus is positive and leads to higher aspirations in the future and
59 vice versa. This process is called *learning*. On the other hand, current decisions are “affected” by
60 previous interaction with other players. Thus, any donation received by recipients have an influence
61 in what they will donate in future; we call this effect *habituation* or *herding*. Most importantly in
62 our setting, and in absence of noise, donations are bounded by aspirations, in the sense that subjects
63 cannot exceed their own aspiration level when making a donation.

64 Our model is akin to other theoretical settings in which observed behavior and norms influence
65 behavior. The work of Andrighetto et al. [8], for example, develops an agent-based model in which
66 contributions to a public good are affected by the norm salience, which is updated upon observing
67 the contribution of other members and the past punishment decisions that may include normative
68 messages or judgments on whether such contributions are viewed appropriately (see [22, 23] for other
69 models of social norms and [24, 25] for experiments where subjects can express their disapproval).
70 While subjects also learn from past interactions in our model, a key difference between our models
71 is that we focus on a non-strategic interaction in which subjects update their expectations about
72 generosity and this possibly affects their donations. Hence our paper complements the empirical
73 evidence in [11] where generosity seems to be affected by the social norms. Our contribution is
74 to show that these norms can emerge as the result of updating expectations and aspirations that

75 affect giving; i.e., we consider a dynamic model of reinforcement learning.

76 As we will show, the model summarized above leads to the following results: For any value
77 —positive and smaller than one— of the learning and habituation parameters we find that an
78 overwhelming majority of the players donate about 30% of the pie and, consistently, they expect to
79 receive 30% of the pie as well. There is almost no heterogeneity in the donation of dictators; in
80 order to quantify this result, we have computed the Gini coefficient [26, 27] to measure the degree
81 of diversity in the donations, and found that it is close to 1. Therefore generosity emerges as
82 social norm with almost no deviant subjects. It is quite remarkable that the observed average
83 practically mimics the average result shown in the meta-analysis of 200 dictator game experiments
84 [12]. However, its also important to have in mind that experiments with humans provide certain
85 degree of variability of responses. To capture this heterogeneity, we also consider a stochastic
86 version of the model where subjects with certain probability do not follow the social norm. While
87 small noise does not impact substantially on results (average donation, $\langle d \rangle = 0.37$, Gini coefficient
88 of the distribution of donations, $G = 0.85$) we find that large noise generates a distribution that
89 replicates Engel results in both average and heterogeneity ($\langle d \rangle = 0.27$; $G = 0.71$). The results about
90 expectations are close to those found in our earlier experimental work [19]. We will also show
91 that the results are robust against the existence of envious individuals, but they are very much
92 affected by the presence of selfish individuals or free-riders, that never change their expectations
93 and, consequently, their behavior.

94 Thus, our main message is that learning may explain the emergence and the adherence to a
95 social norm in the society, and that this is indeed confirmed by the successful replication of the
96 experimental results with human in many different environments. In fact, a necessary condition
97 to recover the experimental results is just to let subjects make mistakes and also to be ready to
98 learn. In the following sections we introduce our model in detail, present the results supporting
99 this conclusions, and close the paper by discussing their implications.

100 Methods

101 Let us consider N individuals interacting through a game. The game chosen is the Dictator Game
102 (DG), a two-players degenerate game where the “dictator” player has to decide how to split an
103 endowment Φ between herself and her partner. The recipient is passive and can only accept the
104 “donation”. In the model, individuals play DG games iteratively but they change partner (and
105 possibly role) every round: Each time step, pairs of individuals are randomly chosen among a
106 population of N agents, and roles (dictator D / recipient R) are randomly assigned.

107 The update of strategies is performed each time step, after individuals have played one DG. In
108 this game, we define strategy as the quantity a dictator is going to donate, i.e., the donation D_i of
109 player i (in other words, strategies directly determine actions). Instead of using traditional strategy

110 updating rules such as proportional imitation or Moran-like rules [28], in our model individuals make
 111 decisions based on experiential induction, i.e. they update their strategies by reinforcement learning.
 112 To that end, we have developed a modification of the classical Bush-Mosteller (BM) algorithm [29]
 113 (see also Refs. 30, 31). In our model, only recipients, as a result of the game (dictator decisions),
 114 update their strategy to be used the next time they play the role of dictator. This intends to
 115 represent the fact that, after receiving a donation, agents update their expectations taking into
 116 account how much dictators gave in past games, and then use those expectations to decide on how
 117 much they themselves donate next time they act as dictators.

118 In detail, the algorithm works as follows: As in the original proposal, individuals have an
 119 aspiration level A_i (their expectations), representing the proportion of the endowment they expect
 120 to receive when playing as a recipient. Each individual i playing R (recipient) receives a stimuli
 121 $s_i^R \in [-1, 1]$ as a consequence of her dictator's decisions. When the difference between the donation
 122 received (payoff π_i) and her aspiration level is positive, recipients receive a positive stimuli, and
 123 vice versa, according to

$$s_{i,t}^R = \begin{cases} (\pi_{i,t} - A_{i,t})/(\Phi - A_{i,t}) & \text{if } \Phi \neq A_{i,t}, \\ 0 & \text{if } \Phi = A_{i,t}, \end{cases} \quad (1)$$

124 where Φ is the total amount to split among the players.

125 The stimuli, if positive, increases the willingness to earn more in the next encounter (meaning:
 126 "*I got more than I expected so I should expect to receive more*"), and vice versa, affecting future
 127 expectations. This effect is moderated by a learning rate $l \in [0, 1]$ that balances the contribution
 128 of past experience. The expression for the change in the aspiration level is then

$$A_{i,t+1}^R = \begin{cases} A_{i,t}^R + (\Phi - A_{i,t}^R)ls_{i,t} & \text{if } s_{i,t}^R \geq 0, \\ A_{i,t}^R + A_{i,t}^Rls_{i,t} & \text{if } s_{i,t}^R < 0. \end{cases} \quad (2)$$

129 Now, as we advanced above, expectations originating from interactions as a recipient govern
 130 actions when acting as dictator in the following manner: An individual adapts the donation she is
 131 willing to give when playing as a dictator as a consequence of the donation she just received, incor-
 132 porating an habituation parameter $h \in [0, 1]$ that, similarly to what occurs with the expectations,
 133 balances between their past donation and the donation received (payoff), as shown in eq. 3.

$$D_{i,t+1}^R = (1 - h)D_{i,t}^R + h\pi_{i,t}. \quad (3)$$

134 Equations (1)–(3) above define the basic dynamics of our model: higher donations lead to higher
 135 aspirations and also to higher donations. With such a model, however, there is no feedback from
 136 aspirations to donations and, furthermore, both quantities can take any value in $[0, \Phi]$, which is

137 certainly not realistic (practically nobody donates more than $\Phi/2$). Therefore, to prevent these
 138 problems, we introduce an additional hypothesis in the model: The donation cannot exceed the
 139 amount resulting from subtracting the aspiration of the individual from the endowment; in other
 140 words, the amount kept by a dictator after donating is never lower than her aspiration level, which
 141 is a sensible assumption. In order to ensure this, we introduce the assumption that donations are
 142 bounded:

$$D_{i,t+1}^R = \max\{0, \min[D_{i,t+1}^R, (\Phi - A_{i,t+1}^R)]\} \quad (4)$$

143 Interestingly, we note that this rule makes learning dependent on A_i , thus coupling donations
 144 and aspirations as expected. From Eq. (4) it can be seen that high aspirations allow only for small
 145 increases in donations, where low aspirations allow more freedom for the evolution of donations
 146 according to Eq. (3). This completes the definition of the deterministic version of our model
 147 ingredients and their parameterization, and the corresponding dynamics (summarized also in Fig.
 148 1). Without loss of generality, we will choose $\Phi = 1$ for simplicity hereafter. Next, we present the
 149 results of our model; the code is available upon request.

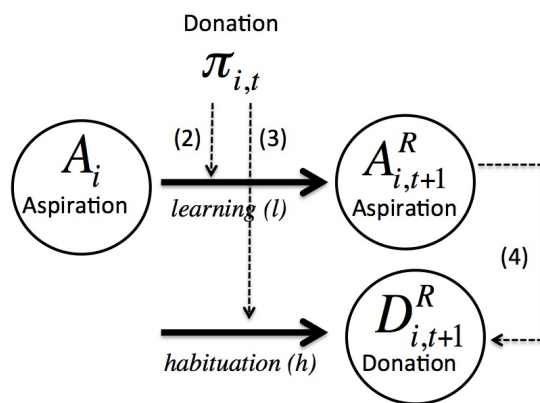


Figure 1: Donations ($\pi_{i,t}$) affect the aspiration level of recipients (i.e., their expectations about generosity) through a learning process, Eq. (2). Donations influence also what subjects will donate in future through an habituation process, Eq. (3). In our model, dictators never give more than what they expect to receive as recipients, thus donations never exceed aspiration levels, Eq. (4).

150 Results

151 Our analysis of the model is based on extensive simulations with $N = 1000$ individuals. Each
 152 simulation run is let to evolve through a transient of 10000 time steps, after which we check whether
 153 an stationary state has been reached, defined by the slope of the averaged donation, measured in a

154 time window of 1000 steps, being inferior to 10^{-4} . If the system has not reached an stationary state,
155 we let it evolve for subsequent time windows of 1000 steps. Each combination of model parameters
156 has been replicated 100 times and results averaged.

157 We explore the space of parameters of the learning algorithm, simulating discrete values for
158 $l \in [0, 1]$ and $h \in [0, 1]$ at intervals of 0.1, but for the shake of simplicity, we will only present
159 the results at intervals of 0.2. The endowment is set to $\Phi = 1$. Individual aspirations A_i are
160 initialised randomly following a uniform distribution $U[0, 1]$ and initial donations are constrained
161 to $D_i = \Phi - A_i$, consistently with our model definition. Our aim is to compare the outcomes of our
162 model with the experimental results reported in the literature.

163 In what follows, we will focus on the general case of the model $l \in [0.2, 0.8]$ and $h \in [0.2, 0.8]$,
164 and we will discuss the limiting cases in the Supplementary Information.

165 **Deterministic model**

166 Figure 2 shows the distribution of aspirations and donations (rounded to the nearest tenth) at the
167 end of the simulations, averaged over 100 replications, for each combination of parameters l and h .

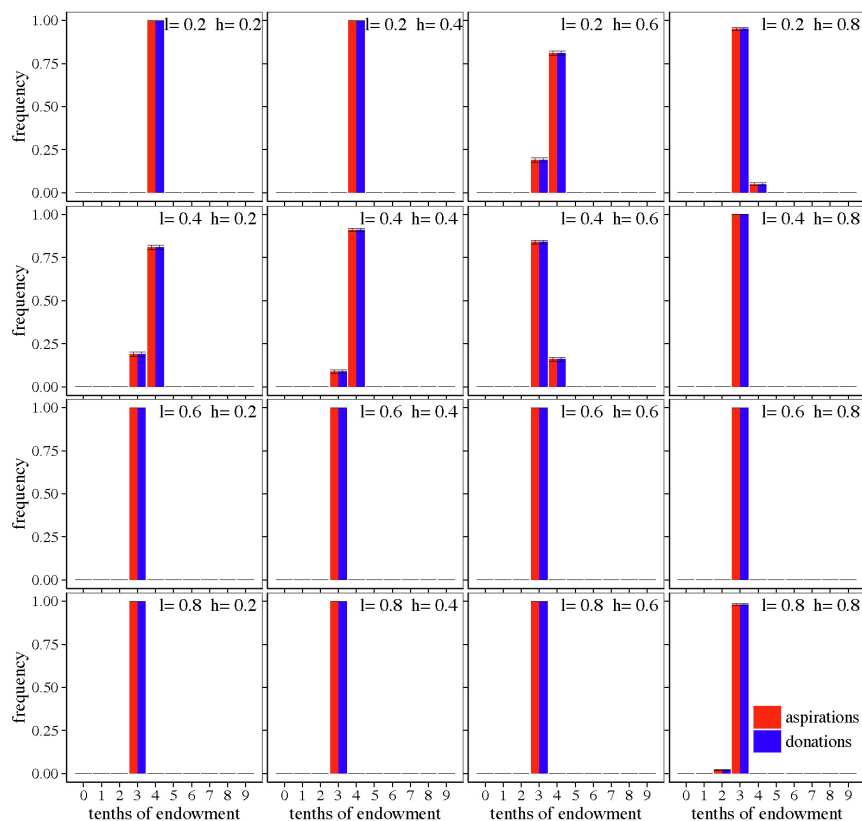


Figure 2: Final averaged distribution of aspirations and donations. Each subplot presents results for a combination of learning rate, l , (in increasing order from top to bottom) and habituation parameter, h , (in increasing order from left to right). Red bars, histograms of aspirations; blue bars, histograms of donations. Bins labelled n of the histograms count the frequency of donations with values verifying $(n/10) \leq D < (n+1)/10$.

168 The first conclusion we can draw from this figure is that, generically for all values of l and h ,
 169 subjects donate nonzero amounts of money and, furthermore, that practically all subjects offer a
 170 donation between 30% and 40% of the pie. As for expectations, what we find is that aspiration
 171 levels in the population are very similar to the observed donations. Interpreting our results on
 172 expectations in terms of social norms, what we observe a notable level of adherence to such a norm
 173 since most subjects are giving a very similar fraction of the pie. We never observe subjects behaving
 174 *selfishly* (donating zero), and only in a few cases they exhibit *fair* or *hyper-fair* behavior (donating
 175 half or more than half of the endowment). We will give a more quantitative characterization of the
 176 average parameters of the distributions below.

177 These results are in general agreement with the experimental observations in so far as most

178 people behave generously, offering nonzero amounts, and also because the mode of the distribution
 179 is close to the fair division. Another feature that our model recovers is that aspirations (expectations
 180 in real life) are strongly correlated with donations, although this is something that is to be expected
 181 as it is built in our premises (agents donate what they expect to receive). However, comparing these
 182 findings in more detail to the experimental results [19], we notice that there is a large discrepancy in
 183 terms of the heterogeneity of the distribution of donations. In our simulations described above we
 184 find practically all agents at the same level of aspiration and donation, whereas in real life there is a
 185 much larger variety of donations and aspiration. It is then clear that, while our deterministic model
 186 seems to be capturing the basics of the behavior in DG, we need to introduce some further ingredient
 187 in order to reproduce better the empirical results. We address this issue in the following subsection
 188 by taking into account the fact that subjects may make mistakes, i.e., designing a stochastic version
 189 of our basic model.

190 Stochastic model

191 As we have just stated, the main problem with the results of the deterministic model is the lack of
 192 variability. To try to improve our model in this direction, we introduce imperfect decision making
 193 (or, as is usually referred to in economics, “trembling hand”), which we implement by adding to
 194 the donations a noise term as follows:

$$D_{i,t+1}^R = (1 + \varepsilon)D_{i,t+1}^R, \quad (5)$$

195 where ε is drawn from a normal distribution $N(0, \delta)$. In terms of the DG context, this represents
 196 the fact that, when making a decision on a donation, people may correct their expectations because
 197 they feel that their experience is leading them to overestimate or underestimate the donation arising
 198 from the social norm. Alternatively, another reason for such a term is that people may simply feel
 199 more or less generous at a given time (realization of the DG) for idiosyncratic reasons. Finally, we
 200 could see the noise term as a kind of “rounding” of the values obtained from the update procedure.
 201 In any event, we want to stress that this is not the same as learning in so far as depending on
 202 the noise the correction of the decision can go against or in favor of the direction marked by the
 203 stimulus at each update. An implication of the introduction of noise is that now donations are
 204 not slaved to aspirations, and therefore if they still match it would be an additional feature of the
 205 experiments that we are reproducing. We will now check whether this new ingredient leads to a
 206 distribution of donations less peaked which would be closer to the empirical distributions.

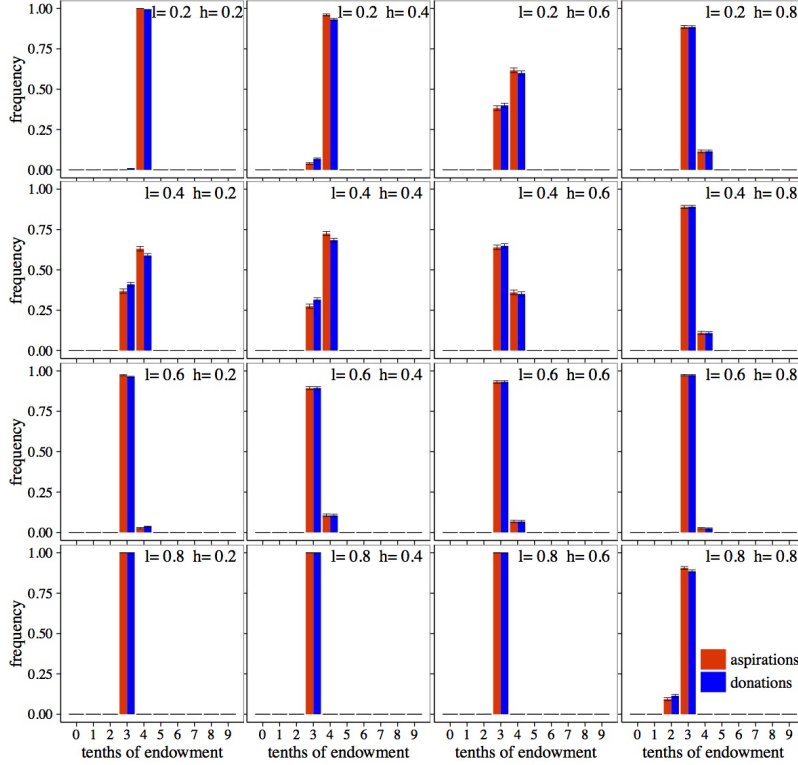


Figure 3: Final averaged distribution of aspirations and donations for $\varepsilon = 0.01$. Each subplot presents results for a combination of learning rate, l , (in increasing order from top to bottom) and habituation parameter, h , (in increasing order from left to right). Red bars, histograms of aspirations; blue bars, histograms of donations. Bins labelled n of the histograms count the frequency of donations with values verifying $(n/10) \leq D < (n+1)/10$. Error bars correspond to the standard deviation arising from averaging over 100 realizations.

207 Figures 3 and 4 present the results for this stochastic version of the model and, as before, we
 208 will discuss the general case of the model ($h \neq \{0, 1\}$ and $l \neq \{0, 1\}$). We will first describe our
 209 results when the trembling hand effect is very weak, which we represent by choosing $\varepsilon = 0.01$.
 210 The corresponding final distributions of aspirations and donations, averaged over 100 realizations,
 211 are shown in Fig. 3. It can be seen in the majority of the parameter space ($0.2 \leq h \leq 0.8$ and
 212 $0.2 \leq l \leq 0.8$; limiting cases show different behavior, see Supplementary Information) that donations
 213 and aspirations have converged to the same distribution of values in each scenario, with almost all
 214 distributions being very sharp, where agents donate and expect to receive between 30% and 40% of
 215 the endowment, which is consistent with the average donation found in experiments and also close
 216 to the "grand mean" found in the meta study by Engel [12]. However, the results are still very

217 similar to the ones in the general case with no trembling hand (Fig. 2) where the distributions of
 218 donations are also peaked and have a mean around the 30% of the endowment. The only minor
 219 differences with the deterministic case arise for low values of l and low to moderate values of h ,
 220 but even then the donations are basically restricted to two intervals. On the other hand, the very
 221 small error bars in our bins indicate that all realizations give approximately the same results, which
 222 implies that we are in fact not very far from the deterministic model. As with the deterministic
 223 model, we will describe more quantitatively the average parameters of the distributions below.

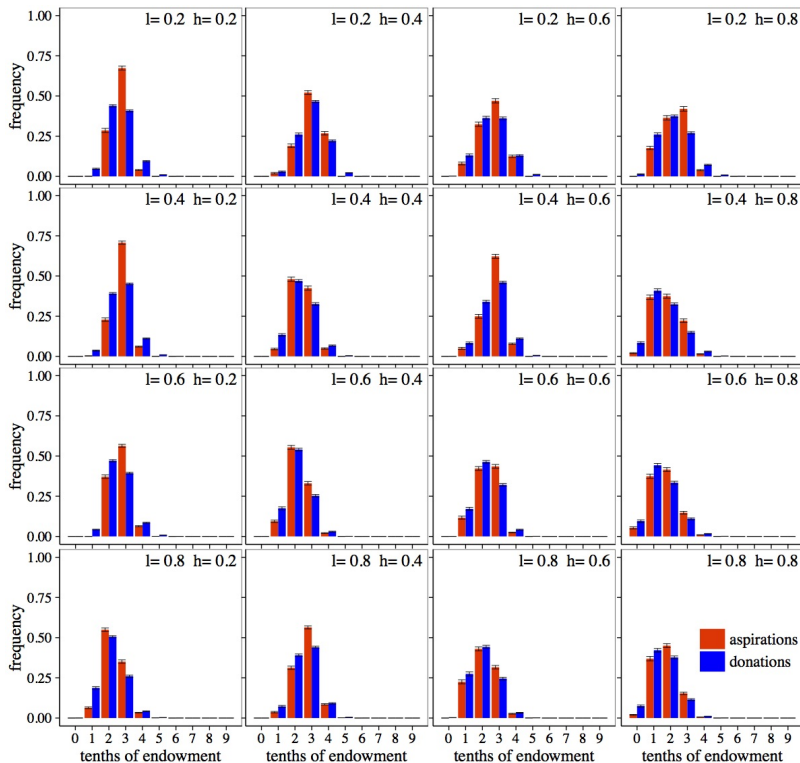


Figure 4: Final averaged distribution of aspirations and donations for $\varepsilon = 0.1$. Each subplot presents results for a combination of learning rate, l , (in increasing order from top to bottom) and habituation parameter, h , (in increasing order from left to right). Red bars, histograms of aspirations; blue bars, histograms of donations. Bins labelled n of the histograms count the frequency of donations with values verifying $(n/10) \leq D < (n+1)/10$. Error bars correspond to the standard deviation arising from averaging over 100 realizations.

224 When we increase the noise component to $\varepsilon = 0.1$ and allow the agents to take more imperfect or
 225 inaccurate decisions, results are shown in Fig 4. As advanced above, here we observe distributions
 226 widening as noise increases, opposite to the outcome of the limiting cases (see Supplementary

Information). It is remarkable that in a large range of the parameter space simulations yield distributions of donations quite close to the ones found in experimental results (cf. Ref. 19). On the other hand, while expectations are still governing the choice of the donated amounts, the correlation is now not exact, also in agreement with the observations from the experiments. In fact, donations are somewhat more spread out than expectations, as was to be expected from the way we introduce the noise in the model. In this case, the results for large habituation, $h = 0.8$, are the ones that reproduce better the experimental results, as they have a small but clearly observable fraction of the population that behaves selfishly, donating nothing. We thus see that our model, when it includes a not so small amount of randomness, reproduces all the main experimental features. In this regard, it is important to point out that other choices for $\varepsilon \in [0.05, 0.2]$ lead to similar histograms, and only when the noise dominates the decisions the model ceases to be a good description of the observations.

Model extensions

In search for more general results, we now consider two additional extensions of the model. First, we look at the effects of having subjects with envious preferences; second, we introduce free-riders in the society, i.e., subjects who always choose to donate zero and never change their strategy. We discuss these two cases separately in the rest of this section. Fig. 5 summarizes the comparison of our results above with the two additional variants.

Envious individuals and disadvantageous inequality

This case intends to represent envious or inequality-averse individuals that would never share more than the half of the pie [32] since they are averse to disadvantageous distributions. According to this, we impose that donations can never be larger than 50% of the pie (in the limit $D_i = A_i$), this bound reflecting disadvantageous inequity-aversion.

$$D_{i,t+1}^R = \min(D_{i,t+1}^R, 0.5) \quad (6)$$

We fix the probability of being inequity-averse, in other words, of behaving as indicated by (eq. 6), to be 0.05, but other percentages of the population lead to very similar behavior. As shown in Fig. 5 C and D, the results are very similar to the general case without restrictions: A (deterministic model) and B (stochastic model with $\varepsilon = 0.10$). However, comparing panels A with C and B with D, we do observe that the whole distribution is skewed to the left, indicating that the whole society becomes somewhat more selfish. This is not unexpected because there are only a few instances in which donations are larger than half of the pie, and therefore the constraint we have just imposed yields minor modifications of the general behavior.

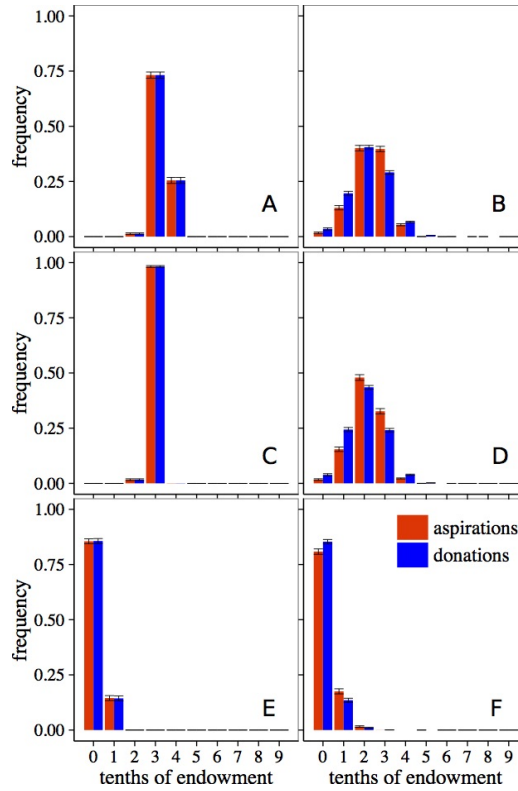


Figure 5: Final averaged distribution of aspirations and donations over all parameters in the general regime. A: deterministic model, donations $\langle d \rangle = 0.37$; $G = 0.85$. B: stochastic model with $\varepsilon = 0.1$, donations $\langle d \rangle = 0.27$; $G = 0.71$. These two panels are in fact an average of those in Figs. 1 and 3. C: disadvantaged inequality with $\varepsilon = 0$, donations $\langle d \rangle = 0.36$; $G = 0.90$. D: disadvantaged inequality with $\varepsilon = 0.1$, donations $\langle d \rangle = 0.25$; $G = 0.73$. E: one free rider, $\varepsilon = 0$, donations $\langle d \rangle = 0.06$; $G = 0.87$. F: one free rider, $\varepsilon = 0.1$, donations $\langle d \rangle = 0.06$; $G = 0.86$.

258 **Existence of free-riders**

259 As a second test of the generality of our results, we add free riders —subjects who always donate
 260 zero— to our population. Actually, the novel ingredient is not that there are selfish individuals:
 261 as we always initialize our simulations randomly, there are some selfish individuals in the previous
 262 results. What we are doing now is to generate a separate fraction of the initial population whose
 263 donation is zero, and choose the donations of the rest from a uniform distribution as before. The
 264 key point here is that the individuals that have been specifically selected to donate zero never update
 265 their donation according to their expectations or, in other words, they do not follow any social norm
 266 based on them. This amounts to saying that they are not only free-riders, but obstinate free-riders.

267 Our results in this respect are quite dramatic (see Fig. 5 E and F): We find that the introduction
268 of one single free-riding is enough to destroy the social norm since every single player become selfish.
269 This is true for most combinations of parameters, except for low habituation parameter (not shown).
270 Even then, the histogram is largely skewed towards zero donations. The social norm changes from
271 being generous to be completely selfish since all players end up donating zero (and expecting zero).
272 In the case of low values of habituation, subjects are less influenced by the interaction with the
273 free-rider, and are able to maintain positive (but small) expectations and donations. It is also
274 important to note that once a social norm is sufficiently widespread, subjects do not change their
275 behaviour easily, and that is what makes the low habituation distribution less selfish. In any
276 event, as we anticipated, the key mechanism here is that these special free riders refuse to adapt
277 their expectations irrespective of their interactions, and are therefore actively counteracting the
278 establishment of a social norm. This finding supports the view that expectations are fragile, in so
279 far as they need to be constantly confirmed in order to allow subjects to accurately predict the
280 action of others. Observing individuals that constantly go against the norm, like the free-riders we
281 are introducing here, has the effect of making those expectations feeble and unreliable. Interestingly,
282 if subjects that never update their donations have positive values for them, they have a similar
283 capacity to attract the behavior of the rest, showing that what is important is the fact that some
284 people do not follow the norm and not in which direction they go against it. Therefore, learning of
285 all agents arises as a key ingredient to support generosity by avoiding the existence of impenitent
286 free-riders.

287 Discussion

288 In this work we presented a very simple model that explains how people behave in dictator games by
289 introducing the idea that donations are driven from expectations. This mechanism works affecting
290 both our donations, which are modified to be closer to the ones we receive, and our expectations,
291 which also reflect the amounts we actually receive. In turn, expectations affect donations by impos-
292 ing an upper bound on the amounts we are willing to donate, leading to a coupled evolution of both
293 parameters. With these simple and quite natural assumptions, the model predicts that people will
294 donate sizable amounts of the pie in the stationary regime, while at the same time by construction
295 their expectations will be aligned with their donations. These two results are in excellent agreement
296 with experimental observations [12, 19]. Notwithstanding, we have also found that to recover the
297 diversity of behaviors arising from the experiments we need to introduce some level of noise, or
298 subjects whose hands tremble when they have to decide. When donations are allowed to deviate
299 from expectations between a 5% and a 20%, the corresponding stochastic model predictions are
300 very closely aligned with real behaviors. This in turn makes the connection between expectations
301 and donations less perfect, which is also in good agreement with the observations.

302 Our model is based on a reinforcement learning dynamics, in which the payoff of an action
303 constitutes a stimulus which agents subsequently use to update their strategies (which, in this
304 specific paper, coincide with their actions). The success of this dynamics in explaining the results
305 of different experiments beyond the current one, namely Prisoner’s Dilemma [33] or Public Good
306 games [34, 35] suggests that this type of learning is indeed used by us in many situations. In fact,
307 in Ref. 33 it was shown that reinforcement learning was the only rule (among quite a few that
308 have been used in evolutionary models, see Ref. 28 for a description of those) that gave rise to a
309 behavior known as moody conditional cooperation (the probability of cooperation is larger when
310 others cooperated and also depends on the subject’s previous choice of cooperation or defection). In
311 addition, reinforcement learning can in fact be a proximate mechanism to explain moody conditional
312 cooperation [35], as it allows to directly reproduce the experimental results. On the other hand,
313 in terms of the interpretation of reinforcement learning, our two parameters have a clear bearing
314 on actual behavior: The habituation parameter h is akin to *herding* (albeit it can also be thought
315 as normative conformity), implying that when h is low h agents do not care much about what
316 other people do when they make their own decisions. The learning rate l reflects how subjects
317 adapt their expectations to the real environment, with low or high values corresponding to similar
318 adaptability of the agent. While some studies highlight the benefits of these aspects in information
319 acquisition [36, 37], the fact that our model produces quantitatively correct results as compared
320 with the experiments in [19] for most parameters, but not if one of them is absent or too influential
321 tells us that both processes are also important to reconcile with experimental findings on generosity.

322 Another interesting point that our research raises touches upon the relation between social
323 norms, behavior and expectations. In the framework introduced by Bicchieri [6] and discussed
324 in the Introduction of social norms as a combination of empirical and normative expectations, in
325 this paper we are confined to the domain of empirical expectations, but our model is certainly
326 suggestive of a social norm actually driving people’s donations in DG experiments. In fact, we
327 believe that the accuracy of our model and its connection to actual social norms can be further
328 tested by additional experiments, in which the normative expectations of the players could also
329 be measured [38]. If normative expectations would coincide with the empirical expectations (as
330 measured in [19] and as explained by our model), we would have shown that we are indeed in
331 the presence of a true social norm. Such an experimental confirmation would clearly establish
332 that a population with a very diverse range of expectations, with agents evolving according to the
333 reinforcement learning paradigm, ends up converging to a commonly shared social norm of generous
334 behavior. This is a promising result and it opens the door to try to look for further models involving
335 social norms in other contexts. At the same time, our result that generous behavior is robust against
336 individuals averse to disadvantageous inequity, but fragile when individuals do not learn (do not
337 update their expectations or do not follow their expectations) means that, first, some degree of
338 social influence may be desirable, and second, violation of social norms must not be tolerated if the

339 good behavior is to be preserved. This conclusion is certainly not new, but it is further evidence
340 supporting the need for some type of punishment or sanctions to avoid free-riding arising from a
341 different evolutionary model such as reinforcement learning. Our results are thus aligned with the
342 work of Bendor and Swistak on the evolution of norms (see [23] and references therein), where
343 they show that social norms arise from evolutionary game theory considerations under boundedly
344 rational behavior. Clearly, the introduction of mechanisms like ostracism [39] or punishment [40],
345 possibly incorporating reputation [41] is a good candidate to solve or at least alleviate this problem,
346 and that would indeed be the case in our model (removed agentes cannot alter the remaining ones'
347 expectations). Alternatively, direct action on the norm by communication among agents as proposed
348 in [8] can serve to induce generosity while at the same time avoiding sanctions. The fact that most
349 people expect generosity [19] may then be indeed a consequence of this type of mechanisms having
350 been in action through history.

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425 **Acknowledgements**

426 We are thankful to the two anonymous reviewers of this paper for their help in improving the
427 manuscript. This work was partially supported by the EU through FET-Proactive Project DOLFINS
428 (contract no. 640772, AS) and FET-Open Project IBSEN (contract no. 662725, AS), grants ECO2013-
429 44879-R and ECO2016-75575-R from the Ministerio de Economía y Competitividad (Spain), grant
430 FIS2015-64349-P (MINECO/FEDER, UE) and grant P12.SEJ.01436 from Junta de Andalucía
431 (Spain).

432 **Author contributions statement**

433 **MP and AS** conceived the original idea for this research and proposed the model, **MP** designed and
434 carried out the experiments, and **MP, PB-G, IR-L and AS** analyzed, discussed and interpreted the
435 results, proposed additional experiments, and wrote the paper.

436 **Competing financial interests**

437 Authors declare no competing financial interests.